

CS7351 传感系统原理与设计

Principles and Design of Sensing Systems

位置感知 & 定位技术

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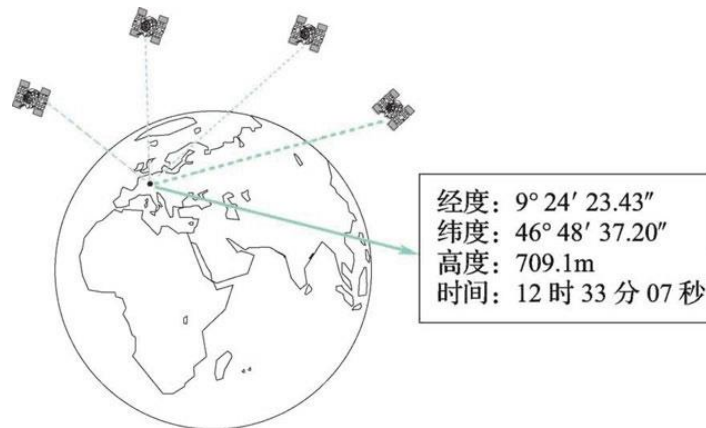
Outline

- Localization Background
- Global Navigation Satellite System (GNSS)
- Indoor Localization
 - Overview
 - Fingerprinting
 - Ultra-wideband
 - Other techniques



Why care about localization?

- Interpreting data relies on real-world location
 - Indoor: where is the motion sensed or temperature measured
 - City-scale: how do measurements change over geographical space





Energy-efficiency is Essential for Localization Technologies

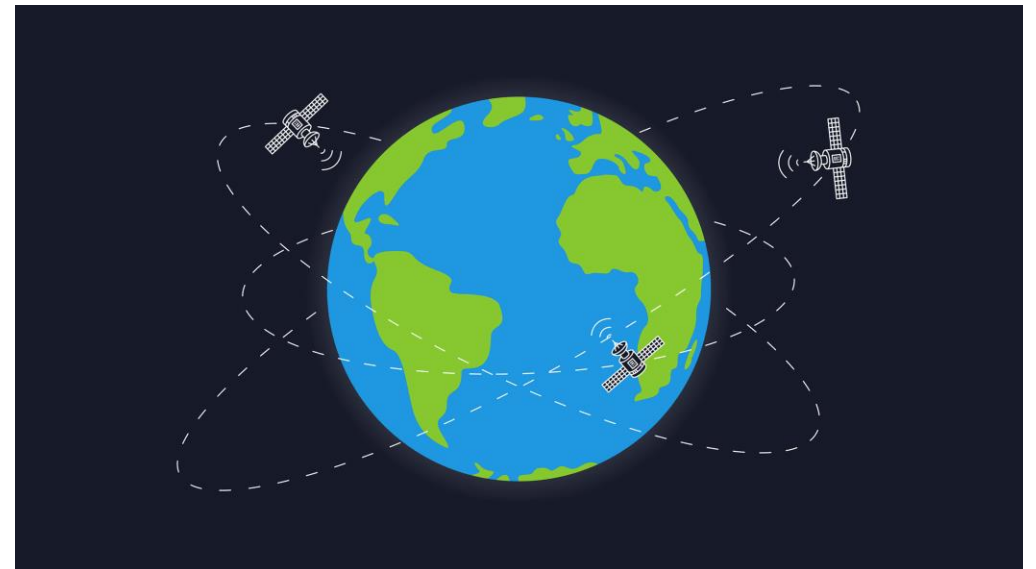
- Embedded devices usually do not have large energy source





Background knowledge?

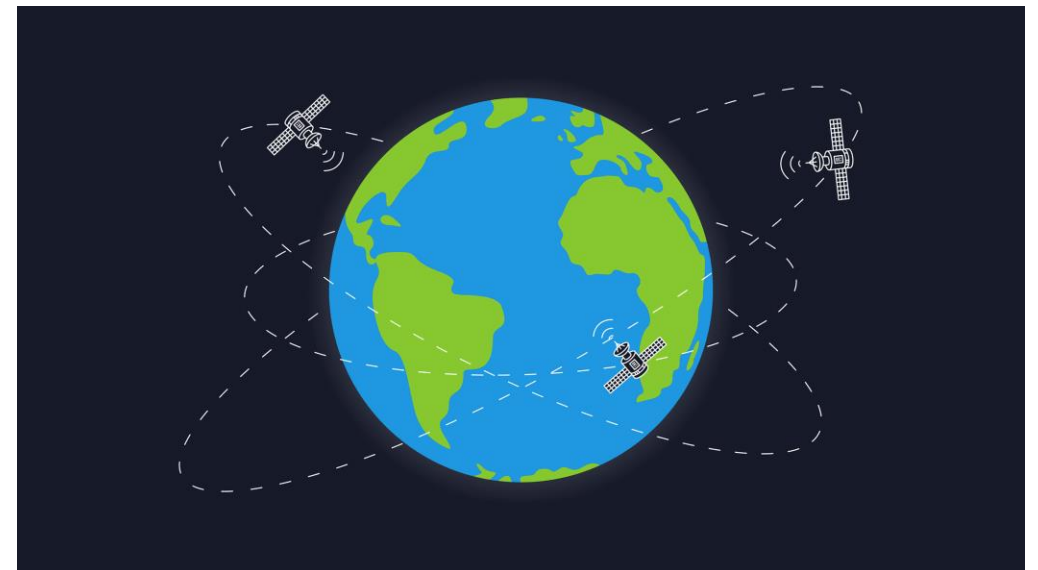
- **How does GPS work?**





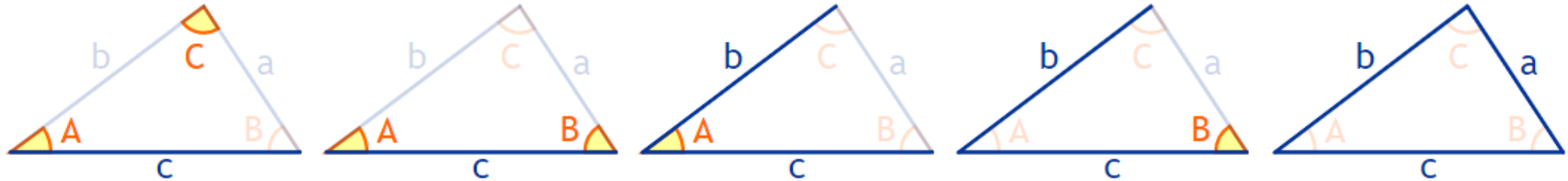
Background knowledge?

- **How does GPS work?**
 - Know the position of all satellites
 - Receive signals from multiple satellites
 - Determine distance from each satellite
 - *Trilateration*

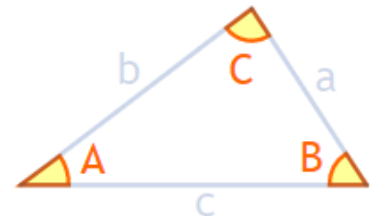




Trigonometry



- 根据三角函数求解三角形：A triangle can be solved by knowing one of the following **3** features
 - Three sides
 - Two sides and any angle
 - Two angles and any side
- Three angles gets the type of the triangle, but not the size
 - Need at least one side to determine size





Trilateration

- **Trilateration (三边定位)** : Determine the distance from each beacon, then find position
 - Apply trigonometry (三角函数) to solve triangle with beacons. Requires:
 - 3 lengths (or some angles and lengths)
 - Solve two triangles and get 3D position





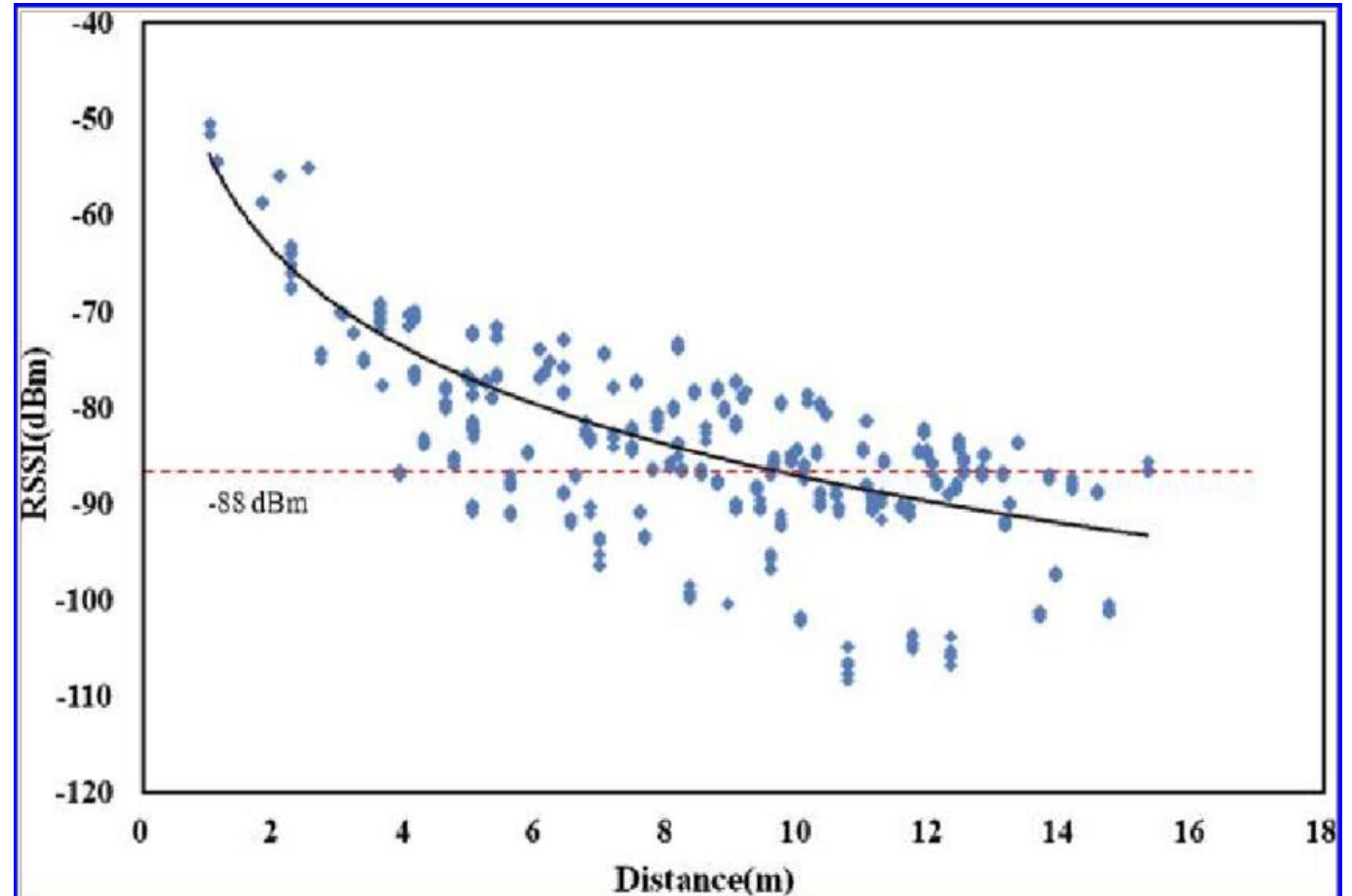
Determining distance

- Making trilateration work requires **distance measurements**
- Techniques
 - RSSI (received signal strength indicator, 即信号强度)
 - ToF (Time of Flight, 即时间差)



RSSI-based distance measurement

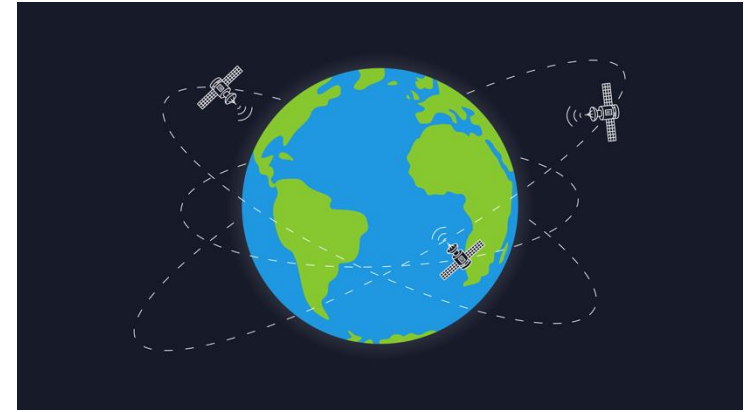
- Distance is not the only factor of pathloss





Time of flight

- Determine distance by knowing:
 - Exact position of anchors
 - Transmit time
 - Receive time
 - Signal velocity (i.e. speed of light)

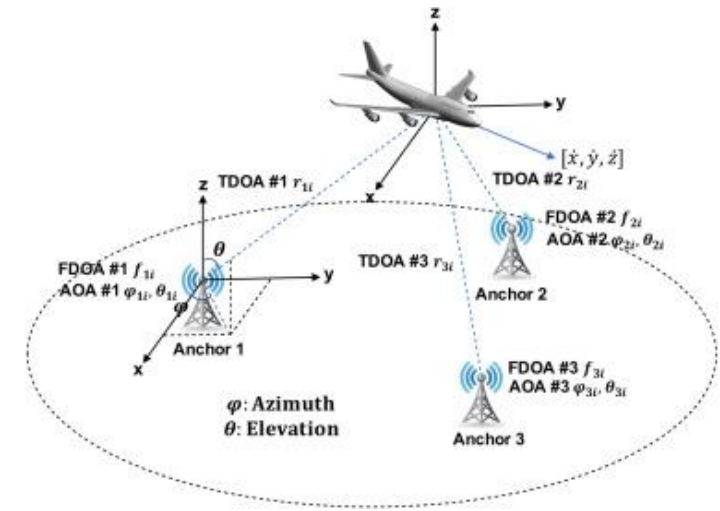


- Requires time synchronization between infrastructure and device
 - Synchronization must be accurate: **$1\ \mu\text{s} = 300\ \text{meters}$**



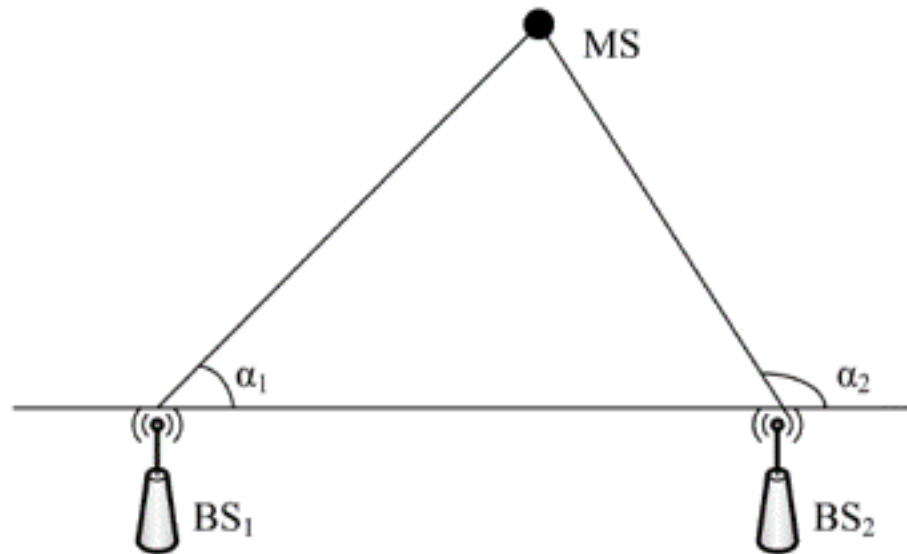
Time difference of arrival (TDoA)

- Device transmits and infrastructure receives transmission
 - Multiple infrastructure nodes receive at different times
- Determine distance by knowing the following stats
 - Exact position of infrastructure
 - Time of arrival at **2** different locations
 - Signal velocity (i.e. speed of light)
- Doesn't require synchronization with infrastructure
 - Still requires synchronization **between infrastructure nodes**
 - Does require device to transmit loud enough for





Angle of Arrival (AoA)



- The locations of at least two anchors should be determined.
- The angle measurement should be accurate.
- Be aware of the symmetrical ambiguity



Real-world complication: Accuracy !

- No distance measurement will be perfect
- Trilateration will not be perfect either



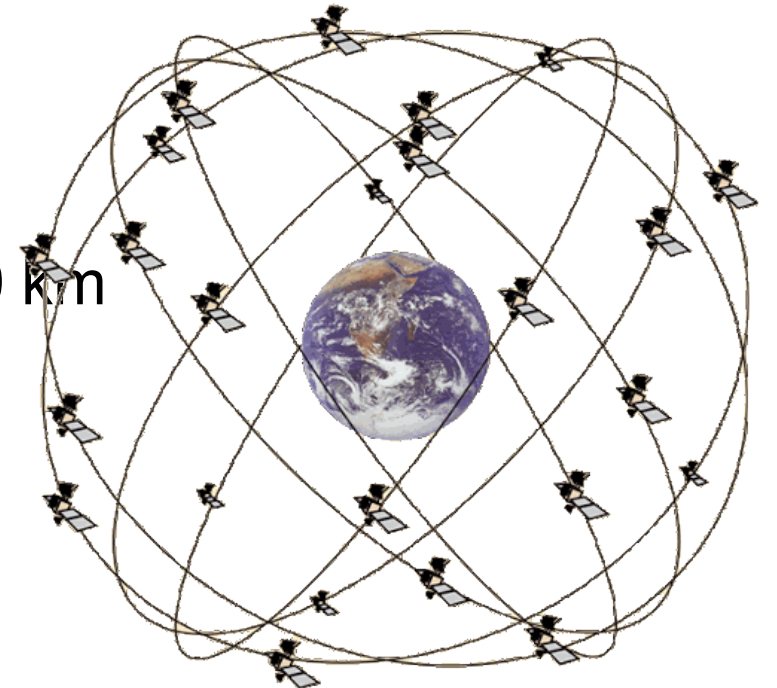
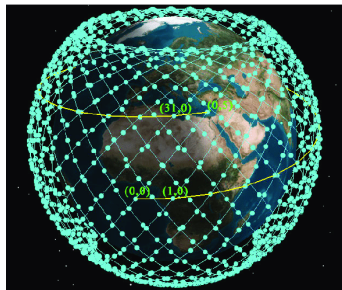
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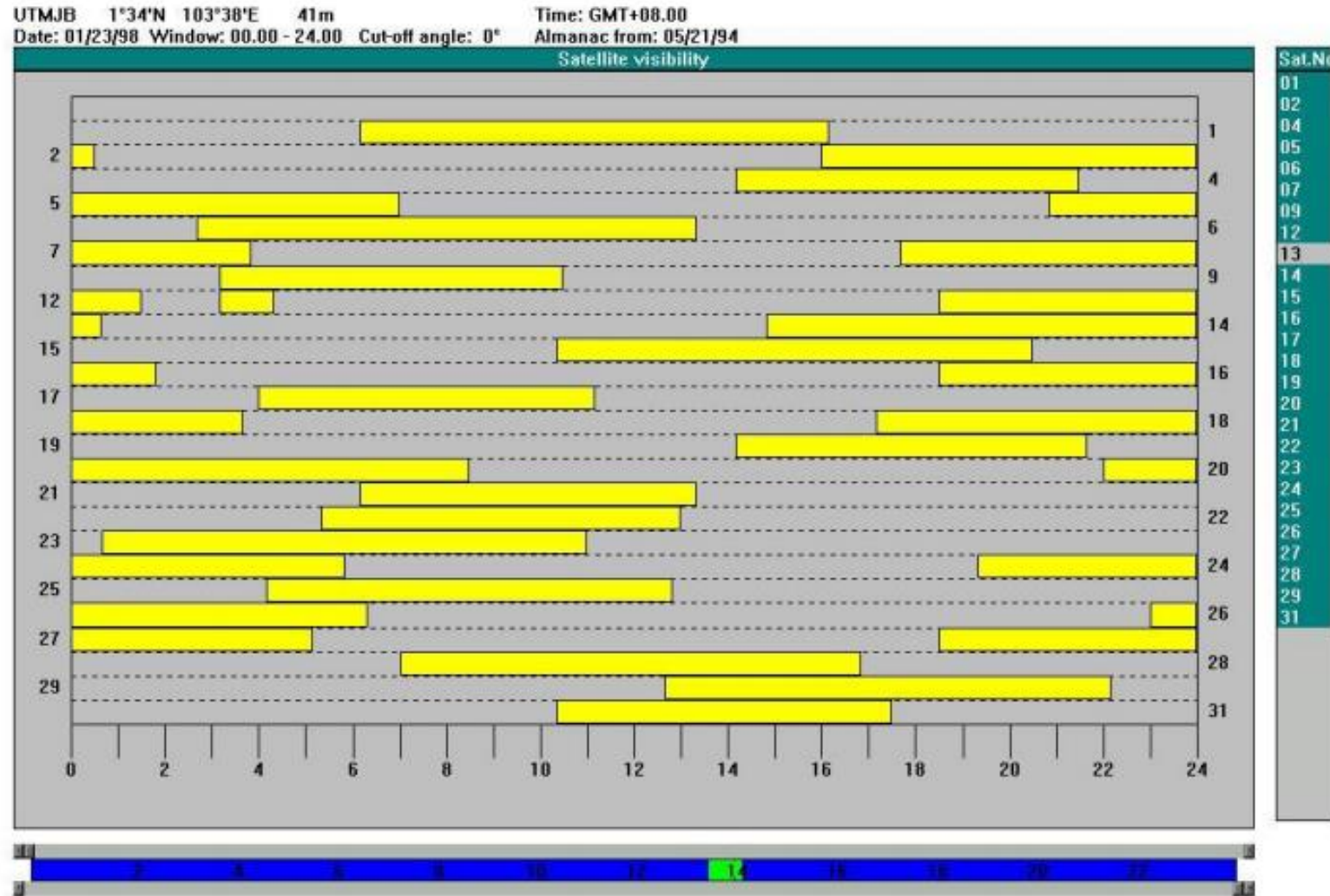


GPS overview

- Trilateration using Time of Flight from at least 4 satellites
- Satellites placed in Medium Earth Orbit (中地球轨道, 离地高度 20,000 km- 35,786 km)
 - Orbit earth twice per day
 - Placed such that 4 are in view everywhere
 - **Starlink** is not for localization, orbit height~550 km



Satellite visibility overhead



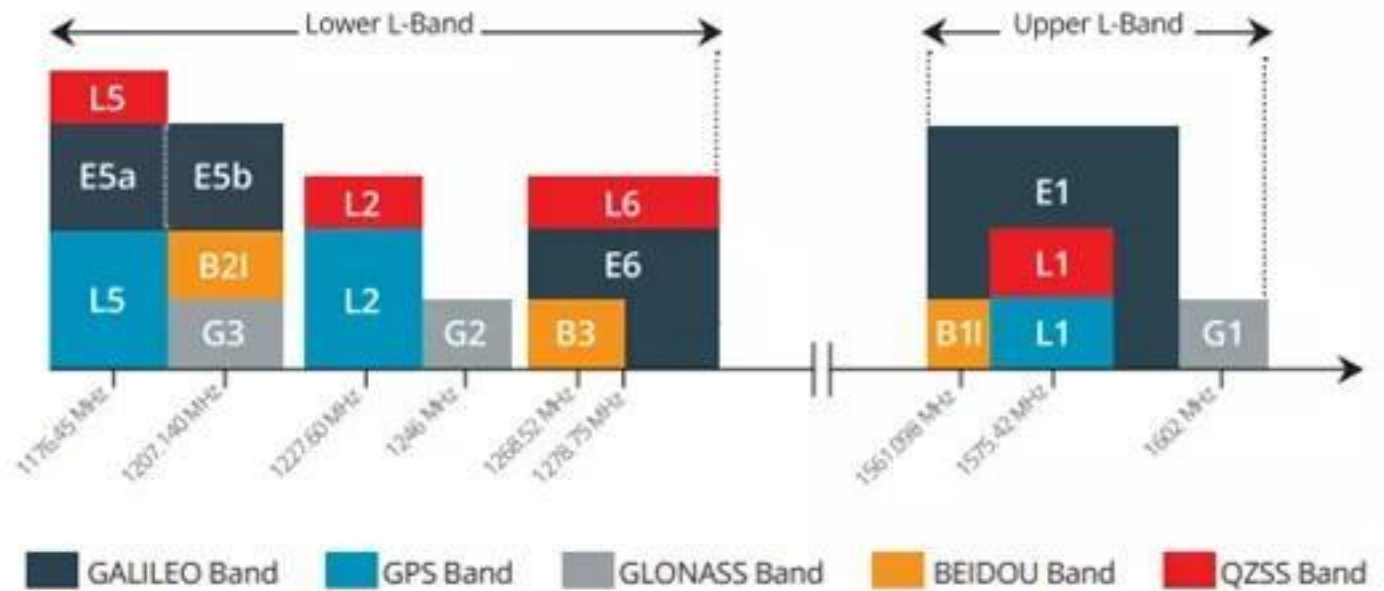


GPS PHY

- GPS frequency
 - 1.2 GHz and 1.5 GHz
 - 10-15 MHz bandwidth

- BPSK modulation

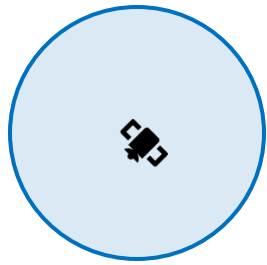
- Signal has to travel 20,000 km, but most of that is through space
 - Tx power 25 Watts (44 dBm)
 - Rx sensitivity -140 dBm to -160 dBm (50 bps data rate)
 - ~200 dBm total link budget



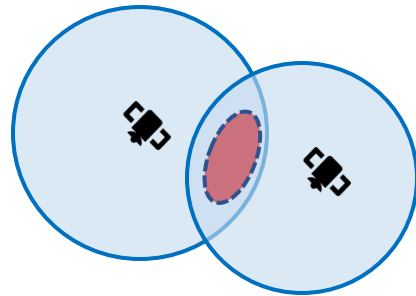
知乎 @GNSS关注学习



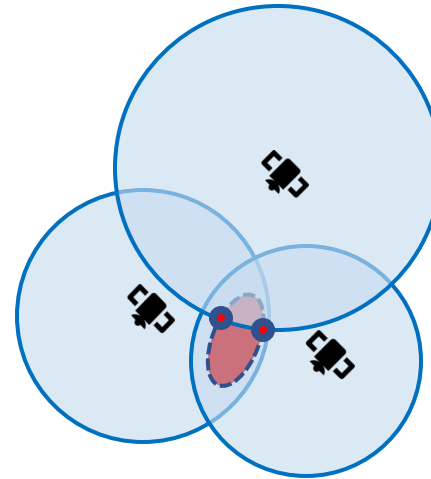
How Many Satellite(s) are Needed?



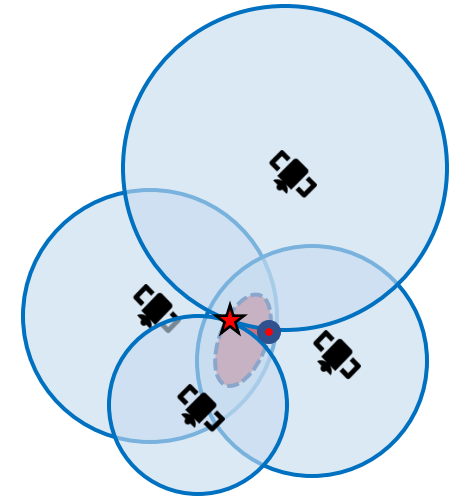
Finding a sphere



Locating a surface



Locating two points



Finding the point

- Trilateraization

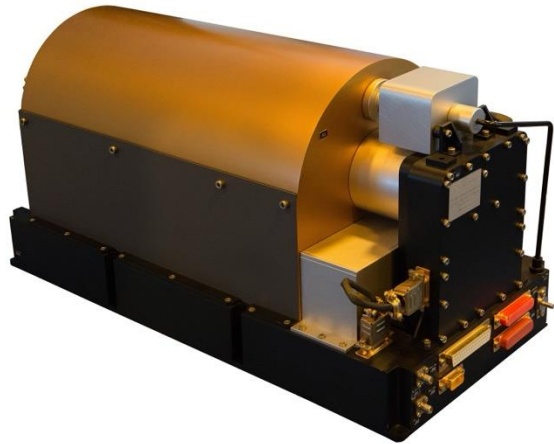
$$\begin{aligned}(x - x_1)^2 + (y - y_1)^2 + (z - z_1)^2 &= c\Delta T_1 \\(x - x_2)^2 + (y - y_2)^2 + (z - z_2)^2 &= c\Delta T_2 \\(x - x_3)^2 + (y - y_3)^2 + (z - z_3)^2 &= c\Delta T_3\end{aligned}$$

- Three satellites can narrow down the search space, why need four?

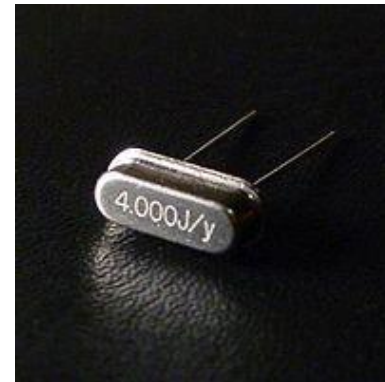


The Problem of ΔT

- Atomic clock (铯原子钟) vs quartz crystal resonator (晶体谐振器)



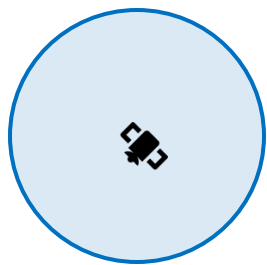
ESA Galileo satellites,
30 ns accuracy 10^{-9}
seconds



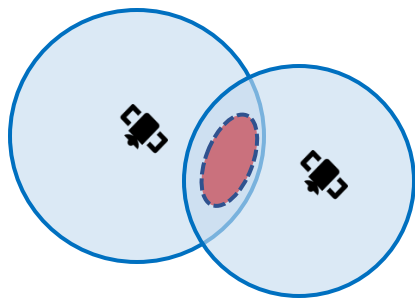
± 20 seconds/month



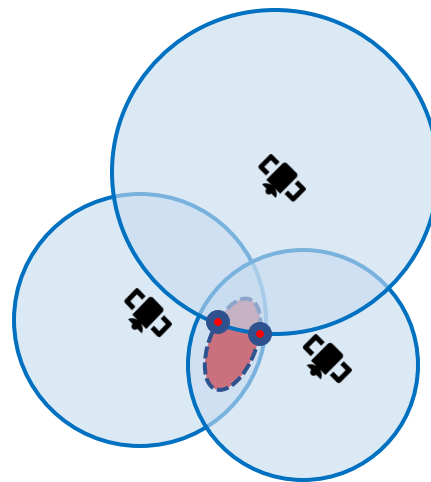
Why Need 4 Satellites for Localization?



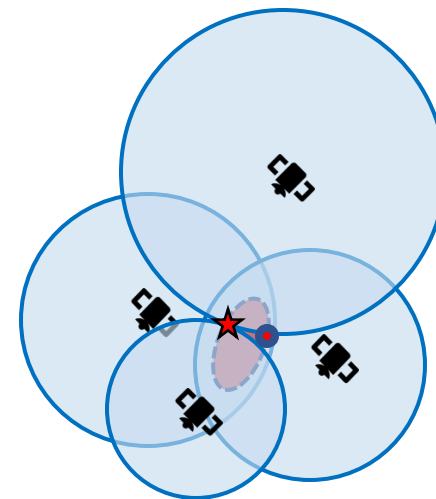
Finding a sphere



Locating a surface



Locating two points



Finding the point

- Trilateraization

$$\begin{aligned}(x - x_1)^2 + (y - y_1)^2 + (z - z_1)^2 &= c(t_{rx} - t_{tx,1}) \\(x - x_2)^2 + (y - y_2)^2 + (z - z_2)^2 &= c(t_{rx} - t_{tx,2}) \\(x - x_3)^2 + (y - y_3)^2 + (z - z_3)^2 &= c(t_{rx} - t_{tx,3}) \\(x - x_4)^2 + (y - y_4)^2 + (z - z_4)^2 &= c(t_{rx} - t_{tx,4})\end{aligned}$$

接收设备时间

卫星, 铯原子钟时间

直接使用 t_{rx} 误差会很大!



Additional GPS data

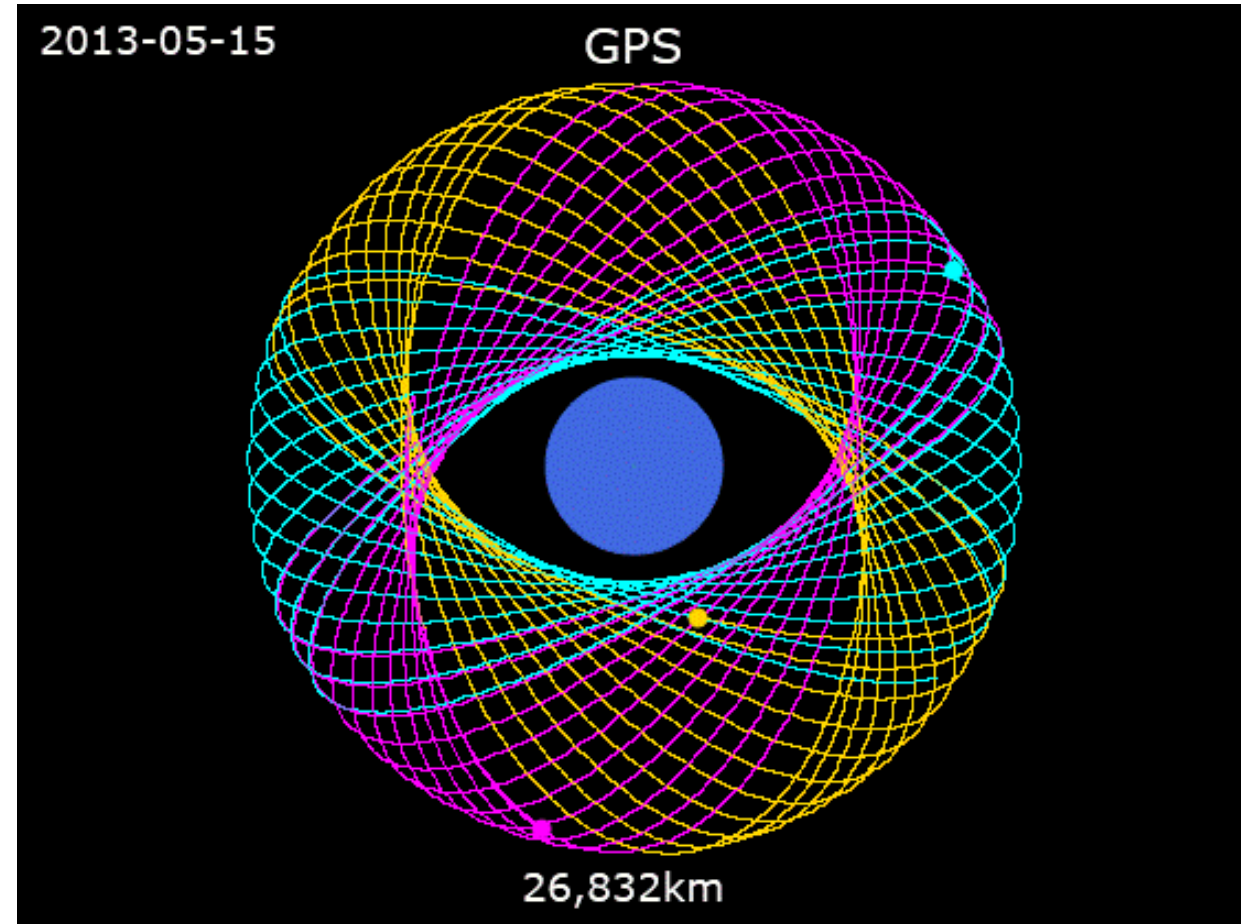
- Receiver needs to know additional information
 - Current time
 - Coordinate of each satellite
- GPS transmission has this data layered on top (50 bps)
 - Listening for 12.5 minutes gets all satellites' positions
 - Known as almanac (历书)
 - Valid for up to two weeks
- Cold-start for an embedded device takes significant time



Satellite Almanac

卫星历书

- 为卫星轨道参数，用来估算卫星概略位置、修正电离层误差以及了解卫星的状态（健康状况），传送周期为12.5分钟。



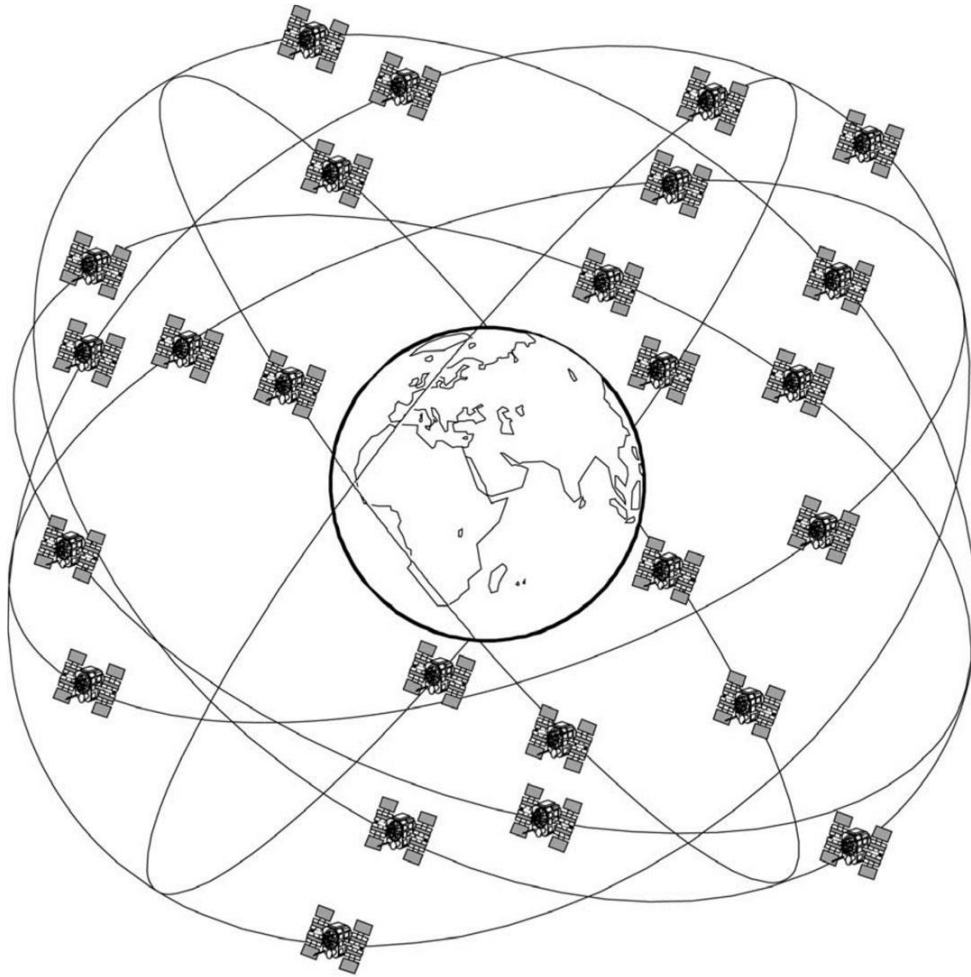


Deployment of Different GNSS Systems

系统	GPS 	GLONASS 	Galileo 	北斗 
Initialization year	1985	2000	2019	2020
Number of units	31	24	30	55
Localization accuracy (civilian use)	~ 3 m	~ 3m	~ 2m	~2m



Deployment of Different GNSS Systems





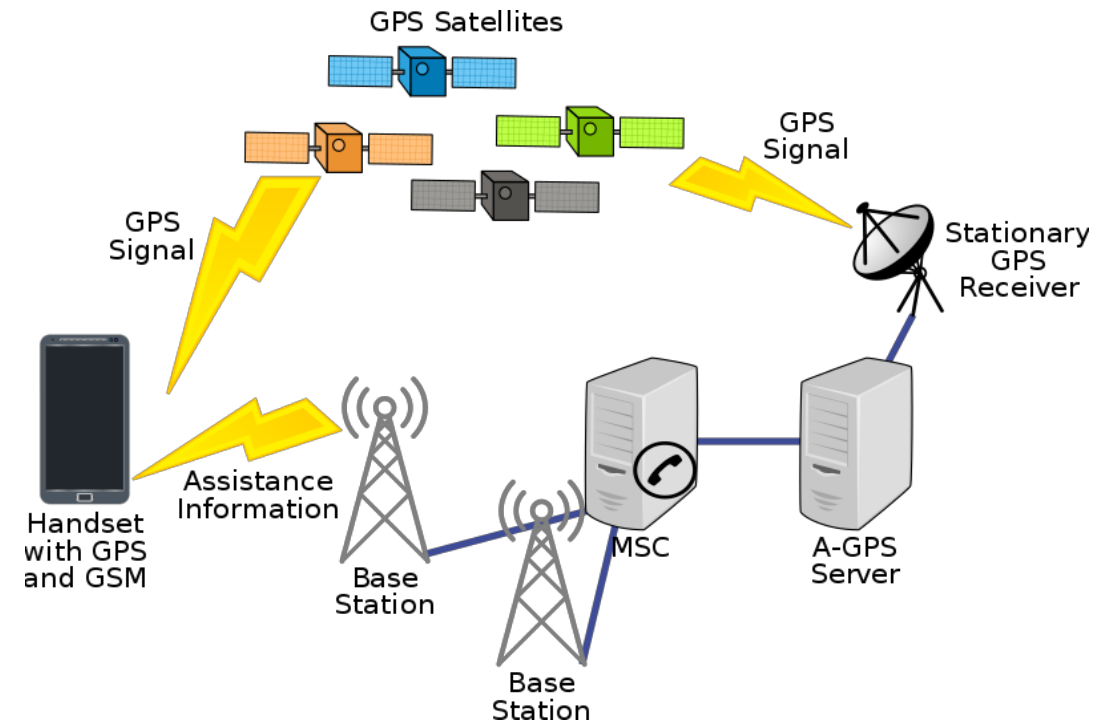
Question

- How would you make a system connect to GPS faster?
 - Cell phones take 12.5 minutes to get a fix after booting



Assisted GNSS

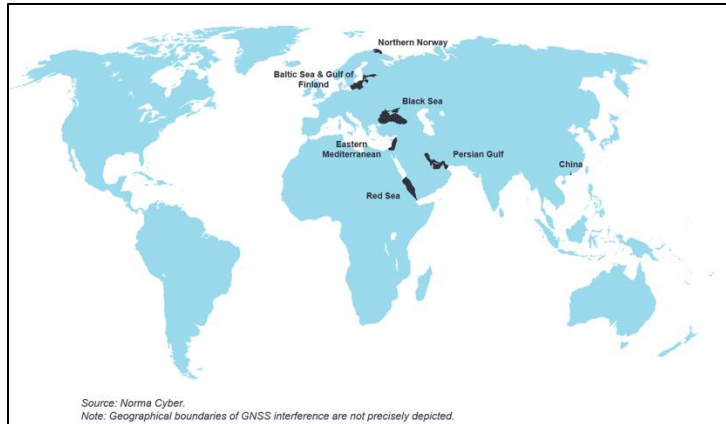
- How is cell phone GNSS so quick?
 - Download almanac from the internet (only 1.8 kB)
- Bootstrap location information
 - Cell towers can give coarse position





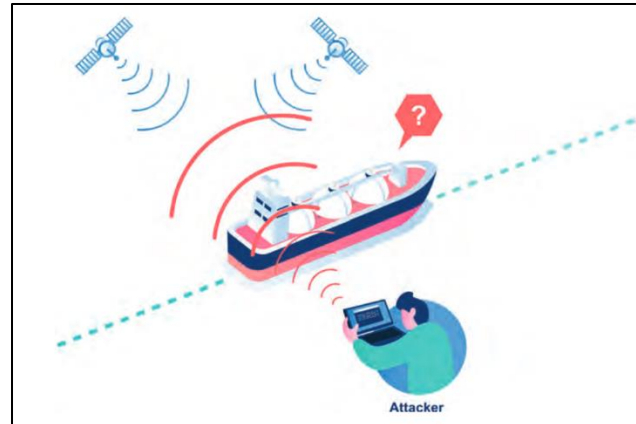
Is there any Security Loophole of GNSS?

Satellite



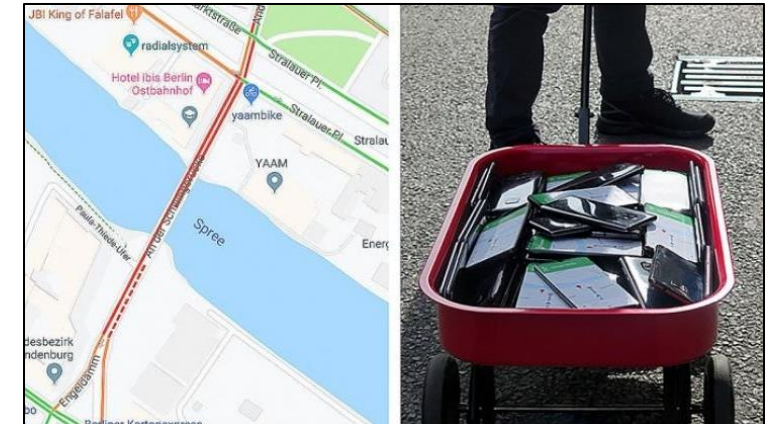
A growing number of regions globally have experienced GNSS interference throughout 2025

Link



Jamming

User



"Google Map Hack! Man uses 99 smartphones to 'fake' traffic"